## SOLVED EXERCISE 3.2

- If y varies directly as x, and y = 8 when x = 1, find
  - (i) y in terms of x

Solution:

Given that y varies directly as x.

Therefore

$$y = kx$$
 (i)

Where k is constant of variation.

Put x = 2 and y = 8 in eq. (i), we have

$$8 = k(2)$$

$$2k = 8$$

$$\Rightarrow$$

$$k = 4$$

Put k = 4 in eq. (i), we get

$$y = 4x$$
.

(ii) y when x = 5

Solution:

Given that y varies directly as x.

. Therefore

y 
$$\propto$$
 x

$$y = kx ___(i)$$

Where k is constant of variation.

Put x = 2 and y = 4 in eq. (i), we have

$$8 = k(2)$$

$$2k = 8$$

$$\Rightarrow$$

$$\Rightarrow$$
  $k = 4$ 

Put k = 4 and x = 5 in eq. (i), we get

$$y = (50(4) = 20)$$

(iii) x when y = 28

Solution:

Given that y varies directly as x.

Therefore

$$y = kx$$
 (i)

Where k is constant of variation.

Put x = 2 and y = 8 in eq. (i), we have

$$8 = k (2)$$
or  $2k = 8$ 

$$\Rightarrow k = 4$$
Put  $k = 4$  and  $y = 28$  in eq. (i), we get
$$28 = 4x$$
or  $4x = 28$ 

$$\Rightarrow x = 7$$

#### 2. If $y \propto x$ , and y = 7 when x = 3 find

#### (i) y in terms of x

Solution:

Given that y varies directly as x.

$$\Rightarrow$$

$$y = kx$$
 \_\_\_\_(i)

Where k is constant of variation.

Put x = .3 and y = 7 in eq. (i), we have

$$7 = k(3)$$

$$3k = 7$$

$$\zeta = \frac{7}{3}$$

Put 
$$k = \frac{7}{3}$$
 in eq. (i), we get

$$y=\frac{7}{3}x.$$

## (ii) x when y = 35 and y when x = 18

Solution:

Given that y varies directly as x.

Therefore

$$y = kx$$
 \_\_\_\_ (i)

Where k is constant of variation.

Put x = 3 and y = 7 in eq. (i), we have

$$7=k(3)$$

$$3k = 7$$

$$\zeta = \frac{7}{3}$$

Put  $k = \frac{7}{3}$  and y = 35 in eq. (i), we get

$$35 = \frac{7}{3}x$$

$$x = 35 \times \frac{7}{3}$$

$$x = 5 \times 3 = 15$$
Put  $k = \frac{7}{3}$  and  $x = 18$  in eq. (i), we get
$$y = \left(\frac{7}{3}\right)(18)$$

 $y = 7 \times 6 = 42$ 

3. If  $R \propto T$  and R = 5 when r = 8, find the equation connecting R and T. Also find R when T = 64 and F when R = 20.

Solution:

4. If  $\propto T^2$  and R = 8 when T = 3, find R when T = 6.

Solution:

or 
$$9k = 8$$

$$\Rightarrow k = \frac{8}{9}$$

$$k = \frac{8}{9}$$

$$k = \frac{8}{9}$$

Put 
$$k = \frac{8}{9}$$
 T = 6 in eq. (i), we get
$$R = \left(\frac{8}{9}\right)(6)^{2}$$

$$R = \frac{8}{9} \times 36 - 9 \times 4 - 32$$

$$R = \frac{8}{9} \times 36 = 8 \times 4 = 32$$

5: If  $V \propto R^3$  and V = 5 when R = 3, find R, when V = 625. Solution:

Given that 
$$V \propto R^3$$
  
 $\Rightarrow V = KR^3$   
Put  $V = 5$  and  $k = 3$  in eq. (i), we get  
 $5 = k (3)^3$   
 $5 = 27 k$   
or  $27 = k 5$   
 $\Rightarrow k = \frac{5}{27}$   
Put  $k = \frac{5}{27}$  and  $V = 625$  in eq. (i), we get  
 $625 = \frac{5}{27} R^3$   
or  $\frac{5}{27} R^3 = 625$   
 $R^3 = 625 \times \frac{27}{5}$   
 $R^3 = 125 \times 27$   
 $R^3 = 5^3 \times 3^3$   
 $R^3 = (5 \times 3)^3$ 

6. If w varies directly as  $u^3$  and w = 81 when u = 3. Find w, when u = 5. Solution:

Given that 
$$w \propto u^3$$
  
 $\Rightarrow w = ku^3$  (i)  
Put  $w = 81$  and  $u = 3$  in eq. (i), we get  
 $81 = k (3)^3$   
 $81 = 27 k$ 

 $R = 5 \times 3 = 15$ 

or 
$$27 k = 81$$
  
 $\Rightarrow k = 3$   
Put  $k = 3$  and  $u = 5$  in eq (i), we get  
 $W = (3)(5)^3$   
 $W = 3 \times 125 = 375$ 

7. If y varies inversely as x and y = 7 when x = 2, find y when x = 126.

Solution:

Given that 
$$y \propto \frac{1}{x} \Rightarrow y = \frac{k}{x}$$
 \_\_\_\_\_(i)

Put y = 7 and x = 2 in eq. (i), we get

$$7 = \frac{k}{2}$$

$$k = 14$$

Put k = 14 and x = 126 in eq. (i), we get.

$$y = \frac{14}{126} \Rightarrow y = \frac{1}{9}$$

8. If  $y \propto \frac{1}{x}$  and y = 4 when x = 3, find x when y = 24.

Solution:

Given that 
$$y \propto \frac{1}{\lambda}$$

$$\Rightarrow y = \frac{k}{x}$$
 (i)

Put y = 4 and x = 3 in eq. (i), we get

$$4=\frac{k}{3}$$

$$k = 12$$

Put k = 12 and y = 24 in eq. (i), we get

$$24 = \frac{12}{x}$$

$$x = \frac{12}{24} = \frac{1}{2}$$

9. If  $y \propto \frac{1}{z}$  and w = 5 when z = 7, find w when  $z = \frac{175}{4}$ .

Solution:

Given that 
$$\mathbf{w} \propto \frac{1}{z}$$

$$\Rightarrow w = \frac{k}{z}$$
Put w = 5 and z = 7 in eq. (i), we get

Put 
$$k = 35$$
 and  $z = \frac{175}{4}$  in eq. (i), we get

$$w = \frac{35}{175/4}$$

$$w = 35 \times \frac{4}{175}$$

$$w = \frac{4}{5}$$

# 10. $A \propto \frac{1}{r^2}$ and A = 2 when r = 3, find r when A = 72.

Solution:

$$A = \frac{1}{r^2}$$

Put A = 2 and r = 3 in eq. (i), we get

$$2=\frac{k}{(3)^2}$$

$$K = 18$$

Put k = 18 and A = 72 in eq. (i), we get

$$72 = \frac{18}{r^2}$$

$$r^2 = \frac{18}{72}$$

$$r^2 = \frac{1}{4}$$

$$r = \pm \frac{1}{2}$$

11. 
$$a \propto \frac{1}{b^2}$$
 and  $a = 3$  when  $b = 4$ , find a, when  $b = 8$ .

Solution:

Given that 
$$a \propto \frac{1}{b^2}$$

$$\Rightarrow a = \frac{k}{b^2}$$
 (i)

Put a = 3 and, b = 4 in eq. (1), we get

$$3=\frac{k}{\left(4\right)^2}$$

$$3 = \frac{k}{16}$$

$$k = 48$$

Put k = 48 and b = 8 in eq. (i), we get

$$a = \frac{48}{(8)^2} = \frac{48}{64}$$

$$a=\frac{3}{4}$$

12.  $V \propto \frac{1}{r^2}$  and V = 5 when r = 3, find V when r = 6 and r when V = 320.

Salution:

Given that  $V \approx \frac{1}{\epsilon^3}$ 

$$\Rightarrow V = \frac{k}{r^2}$$
 (i)

Put V = 5 and r = 3 in eq. (i), we get

$$5=\frac{k}{\left(3\right)^3}$$

$$5 = \frac{k}{27}$$

$$k = 135$$

Put k = 135 and r = 6 in eq. (i), we get

$$V = \frac{135}{\left(6\right)^3}$$

$$V = \frac{135}{216} = \frac{5}{8}$$

Put K = 135 and Y = 320 in eq. (i), we get

$$320 = \frac{133}{320}$$

$$320 = \frac{135}{320}$$

$$320 = \frac{27}{64}$$

$$320 = \frac{27}{64}$$

$$320 = \frac{27}{64}$$

13.  $m \propto \frac{1}{n^3}$  and m = 2 when n = 4, find m when n = 6 and n when m = 432.

Solution

Given that 
$$m \propto \frac{1}{n^3}$$

$$\Rightarrow m = \frac{k}{n^3}$$
 (i)

Put m = 2 and n = 4 in eq. (i), we get

Put k = 128 and n = 6 in eq. (i), we get

$$m = \frac{+28}{(6)^3}$$

$$m = \frac{128}{216} = \frac{16}{27}$$

Put k = 128 and m = 432 in eq. (i), we get

$$432 = \frac{128}{n^3}$$

$$n^3 = \frac{128}{432}$$

$$n^3 = \frac{8}{27}$$

$$n^3 = \left(\frac{2}{3}\right)^3$$

# Find 3<sup>rd</sup>, 4<sup>th</sup>, mean and continued proportion:

We are already familiar with proportions that if quantities a, b, c and d are in proportion, then a: b:: c: d

i.e., product of extremes = product of means

#### Third Proportional

If three quantities a, b and c are related as a : b :: b : c, then c is called the third proportion.

#### Fourth Proportional

If four quantities a, b, c and d are related as

Then d is called the fourth proportional.

#### Mean Proportional

If three quantities a, b and c are related as a: b:: b: c, then b is called the mean proportional.

#### **Continued Proportion**

If three quantities a, b and c are related as

where a is first, b is the mean and c is the third proportional, then a, b and c are in continued proportion.

#### SOLVED EXERCISE 3.3

# 1. Find a third proportional to

(i) 6, 12

Solution:

Let C be the third proportional, then

: Product of extremes = Product of means

$$6C = 12 \times 12$$

$$6C = 144$$

$$C = \frac{144}{6}$$

$$C = 24$$

(ii) 
$$a^2 - b^2$$
,  $a - b$ 

Solution:

Let C be the third proportional, then

$$a^3: 3a^2:: 3a^2: C$$

Product of extremes = Product of means